NATIONAL TALENT SEARCH EXAMINATION (NTSE-2016) STAGE -1 JHARKHAND STATE: SAT

Date: 08/11/2015

Max. Marks: 100 SOLUTIONS Time allowed: 90 mins

1. A planet had density P, radius R and acceleration due to gravity as g. If the radius of hte planet were doubled, keeping the density same, the acceleration due to gravity at the surface will be:

(1) 4g

(2) 2g

(3) g

(4) g/2

Ans. (2)

Sol. Given, planet's density = P

Planet's radius = R

acceleration due to gravity = g

Let mass of planet = M and volume = $\frac{4}{3}\pi R^3$,

$$P = \frac{M}{\frac{4}{3}\pi R^{3}}, g = \frac{GM}{R^{2}} = \frac{G \times P \times \frac{4}{3}\pi R^{3}}{R^{2}} = G \times P \times \frac{4}{3}\pi R \dots (1)$$

$$g' = \frac{G \times P \times \frac{4}{3} \pi \times 8R^3}{4R^2} = 2\left(G \times P \times \frac{4}{3} \pi R\right) \qquad \dots (2)$$

From equation (1) & (2)

$$g' = 2g$$

2. If the length of a simple pendulum is increased to 4 times its value, its time period will be

(1) halved

(2) doubled

(3) becomes $\sqrt{2}$ time (4) reduces by $\sqrt{2}$

Ans. (2)

Sol. Time period of simple pendulum

$$T = 2\pi \sqrt{\frac{\ell}{g}} \qquad \dots (1$$

If '
$$\ell$$
' is increased by 4 times $T' = 2\pi \sqrt{\frac{4l}{g}} = 2 \times 2\pi \sqrt{\frac{l}{g}}$... (2)

From (1) & (2) T' = 2T

3. At the top of its path a projectile has

(1) no acceleration

(2) acceleration in the upward direction

(3) acceleration in the downward direction

(4) acceleration in the horizontal direction

Ans. (3)

- **Sol.** When object is in projectile motion, acceleration due to gravity act in downward driection at every point of motion.
- **4.** A real and enlarged image can be formed by using a
 - (1) convex mirror

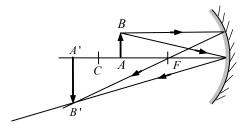
(2) plane mirror

(3) concave mirror

(4) either convex or a plane mirror

Ans. (3)

Sol. In concave mirror when object placed between C&F then real and enlarged image is formed (beyond C).



- **5.** For an incident ray directed towards centre of curvature of a spherical mirror the reflected ray
 - (1) retraces its path

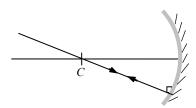
(2) passes through focus

(3) passes through the pole

(4) becomes parallel to the principal axis

Ans. (1)

Sol. When ray directed toward centre of curvature of a spherical mirror it retraces its same path because angle of incidence in that case is zero degree so angle of reflection is also zero.



- **6.** A stone is dropped into a well 44.1 m deep. The sound of splash is heard 0.13 seconds after the stone hits the water. What should be the velocity of sound in air?
 - $(1) 319 \, \text{m/s}$
- (2) 339 m/s
- (3) 359 m/s
- (4) 369 m/s

Ans. (2)

Sol. Well height = 44.1 m, time taken after sound of splash heard = 0.13s

$$S = ut + \frac{1}{2}at^2$$
, $a = 0$

 $44.1 = u \times 0.13$, $u = 339 \, m/s$

- 7. Out of two bulbs 50W 220 V and 100W-220V, which one will glow brighter if
 - (a) connected in series
- (b) when connected in parallel
- (1) (a) 50 W
- (b) 100 W
- (2) (a) 100 W
- (b) 100 W

- (3) (a) 100 W
- (b) 50 W
- (4) noe of the above

Ans. (1)

Sol. In series,
$$P \propto V \propto R \propto \frac{1}{W}$$
 (I = constant)

In series grouping of bulb, bulb of greater rated power dissipates less power and glows dimmer and vice-versa.

$$\underline{\text{In parallel}}\ P \propto I \propto \frac{I}{R} \propto W \quad \text{(V = constant)}$$

In parallel grouping of bulbs, the bulb of greater rated power, dissipates more power. Thus It glows brighter and vice-versa.

- **8.** Energy released per fission of a $_{92}U^{238}$ nucleus is nearly equal to
 - (1) 931 MeV
- (2) 1000 MeV
- (3) 8 MeV
- (d) 800 MeV

Ans. (1)

- **Sol.** Energy released duing fission of $_{92}U^{238}$ is approximately equal to 931.5 Mev. So, the energy released is would be equal to 931 Mev.
- **9.** How many planets are there in our solar system
 - (1)5

(2)7

(3)9

(4)8

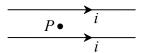
Ans. (4)

Sol. Total No. of planets in solar system = 8, Because pluto is now considered as a dwarf planet and a part of kuiper belt.

- **10.** In house electrical circuits the fuse wire for safety should be of
 - (1) High resistance high melting point
 - (2) Low resistance high melting point
 - (3) Low resistance low melting point
 - (4) High resistance low melting point

Ans. (4)

- **Sol.** The fuse wire should have 'high resistance and low melting, so that it can easily break the circuit if overrated current pass through that circuit.
- **11.** Two wires each carrying current *i* are shwon. The magnetic field at P (midway between the wires) is described by whihe statement?

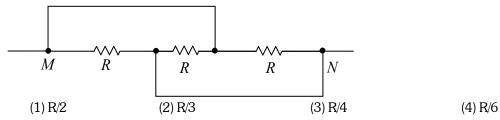


- (1) Magnetic fields are in opposite direction and net field is equal to zero.
- (2) Magnetic fields due to two wires are in the same direction
- (3) Magnetic fields are in opposite direction but net field is not zero
- (4) magnetic fields are in the same direction and equal to two times the field due to one wire.

Ans. (1)

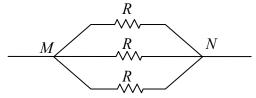
Sol. If both coductors carry current in the same direction then the magnetic field due to upward conductor at a distance $\frac{d}{2}$ (d = distance between two conductor) is equal and in opposite direction to the magnetic field at the same distane due to downward conductor. Hence the net magnetic field at a point exactly half-way between two conductor is zero

12. What is the equivalent resistance of the following arrangement between M and N



Ans. (2)

Sol. In the given circuit on solving, the circuit would appear as

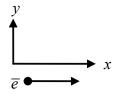


Since all are in parallel, Therefore the eqivalent resistance would be

$$\frac{1}{R_{eq}} = \frac{1}{R} + \frac{1}{R} + \frac{1}{R}, \ \frac{1}{R_{eq}} = \frac{1+1+1}{R}$$

$$R_{eq} = \frac{R}{3}$$

13. An electron moving with uniform velocity in x direction enters



a region of uniform magnetic field along y direction. Whihc of the follwoing quantities is (are) non-zero and remain constant?

- (I) Speed of the electron
- (III) Kinetic energy of the electron
- (1) only I and II
- (3) All four

- (II) Momentum of the electron (magnitude)
- (IV) Force of the electron (magnitude)
- (2) only III and IV
- (4) only II and IV

Ans. (3)

- Sol. As the charge particle enters perpendicular to the magnetic field the force will act perpendicular to the velocity. Thus the particle starts moving in the circular path. As force and displacement are perpendicular to the work done will be zero and kinetic energy will not change. But as it moves to the circular path direction of momentum will change but magnitude is unchanged. Hence speed and force also not changed.
- In the reaction, $SO_2(g) + 2H_2S(g) \rightarrow 2H_2O(L) + S(s)$ the reducing agent is
 - (1) SO_2 (2) H_2O (3) H_2S
- (4) S

Ans. (3)

Sol.
$$\overset{+4}{S}\overset{-2}{O_2}(g) + 2H_2\overset{-2}{S}(g) \longrightarrow 2\overset{+1}{H_2}\overset{-2}{O}(\ell) + \overset{0}{S}(s)$$

oxidation state of sulpher in H_2S is increases, hence oxidation of H_2S takes place, it is R.A

- **15.** Methane on combustion gives
 - (1) CO₂

(2) H₂O

(3) both CO_2 and H_2O

(4) Neither CO_2 nor H_2O

Ans. (3)

- **Sol.** Combustion of methane gives $CO_2 \& H_2O$
- **16.** Which of the following is not an example of single displacement reaction?
 - (1) $CuO + H_2 \rightarrow H_2O + Cu$

- (2) $Zn + CuSO_4 \rightarrow ZnSO_4 + Cu$
- (3) $4NH_3 + 5O_2 \rightarrow 4NO + 6H_2O$
- (4) $Zn + 2HCl \rightarrow ZnCl_2 + H_2$

Ans. (3)

- Sol. It is not single displacement reaction
- 17. 10 ml of a solution of NaOH is found to be completely neutralised by 8 ml of a given solution of HCl. If we take 20 ml of the same solution of NaOH, the amount of HCl solution (the same solution as before) required to neutralise it will be
 - (1) 4 ml
- (2) 8 ml
- (3) 12 ml
- (4) 16 ml

Ans. (4)

- **Sol.** 10 ml NaOH is neutralised by 8ml of HCl
 - \therefore 20 ml NaOH is neutralised by $\frac{8}{10} \times 20 = 16 \text{ ml}$
- **18.** A milkman added a small pinch of baking soda to fresh milk which had pH close to 6. As a result, pH of the medium
 - (1) became close to 2

(2) became close to 4

(3) did not undergo any change

(4) became close to 8

Ans. (4)

- **Sol.** Baking soda is added to become basic and pH increases to 8.
- **19.** Which of the following salts does not contain any water of crystallisation?
 - (1) blue vitriol
- (2) washing soda
- (3) baking soda
- (4) gypsum

Ans.(3)

- Sol. Baking soda does not contant any water of crystallisation
- **20.** Which of the following methods is suitable for preventing an iron frying pan from rusting?
 - (1) Appying greases

(2) Applying paints

(3) Applying a coating of zinc

(4) All of the above

Ans. (3)

Sol. Iron is prevented by different method but from frying pan, it is prevented by coating of Zn.

21.	When iron fillings are heated in a steam of dry hydrogne chloride, the compound formed is $FeCl_x$ where x is				
	(1) 1	(2) 2	(3) 3	(4) 4	
Ans.	(2)				
Sol.	$Fe + 2HCl \longrightarrow FeCl$	$_{2} + H_{2}$			
22 .	Rusting of Iron takes place	e in			
	(1) ordinary water		(2) distilled water		
A	(3) both ordinary and dist	illed water	(4) none of the above		
Ans. Sol.	• •	e in ordinary as well as disti	lled water, (distill water con	tains oxygen dissolved in it)	
23 .	Mg dissolved in hot water		, (,	
	(1) MgO	(2) $Mg(OH)_2$	(3) MgOH	(4) $MgOMg(OH)_2$	
Ans.	(2)				
Sol.	$Mg + 2H_2O \longrightarrow Mg$	$\left(\mathrm{OH}\right)_2 + 2\mathrm{H}_2$			
	In steam water Mg form I	MgO			
24 .	_	om of the vessel is getting b	lackened on the outside, it	means that	
	(1) The food is not cooked	d completely	(2) The fuel is not burning	· · · · ·	
4	(3) The fuel is wet (4) The fuel is burning completely				
Ans. Sol.	• •	nbusion, fuel does not burn	completely which casue bla	ckened the bottom of the vessel.	
				0	
25 .	Identify the functional group presnet in the following compound $CH_3 - CH - CH_2 - C - OH$				
	(1) Aldehyde(3) Carboxyl		(2) Bromine(4) both bromine and cart	and group	
Ans.	-		(4) Ooth bromme and card	oxyi group	
	•	D 0			
Sol.	In given compound CH	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	functional groups are - Br, a	and - COOH.	
26 .	, , ,	nce of the element in a group		(A) (C) (A)	
•	(1) Ca, Sr, Ba	(2) Cu, Au, Ag	(3) N,P,As	(4) Cl, br, l	
Ans.					
Sol.	The correct order is Cu ,	Ag, Au hence Cu, Au, Ag	g is wrong.		
27 .	Increase in the height of t	he plant is due to			
	(1) Auxins	(2) Cytokinins	(3) Gibberellins	(4) Ethylene	
Ans.	s. (1)				
Sol.	Auxin helps in apical shoot development, giving a young tree a more upright form.				
28 .	A sexual reproduction takes place through budding in				

	(1) Amoeba	(2) Cytokinins	(3) Gibberellins	(4) Ethylene			
Ans.	(2)						
Sol.	A sexual mode of reproduction						
29 .	Ginger is						
	(1) Root	(2) Stem	(3) Fruit	(4) None of these			
Ans.(
Sol.	Ginger is rhizome, modified planat stem.						
<i>30.</i>	The liver stores food in the		(O) A11	(4) ATD			
Ans.((1) Glucose	(2) Glycogen	(3) Albumen	(4) ATP			
Sol. 31.	B cells of pancreas release	the help of glycogen synth		liver to take glucose from blood			
	(1) CO ₂		(2) Water				
	(3) Both \rm{CO}_2 and water		(4) Oxygen via air				
Ans.	(2)						
Sol.	Reason: The visible wave	lenght of light traped by PSI	and PS II leads to hte break	down of H_2O into H^+, O_2 and			
	electrons. The ${\rm O}_2{\rm produce}$	ed will be released outside t	ne thalakoid lumene.				
32 .	This is an artificial ecosyst	rem					
	(1) Pond	(2) Crop field	(3) Lake	(4) Forest			
Ans.(
	Pond, lake and forest are t						
33.	Which of the following is a		(O) TI :	(4) (2)			
Ans.((1) Insulin	(2) Cytokinin	(3) Thyroxine	(4) Oestrogen			
Sol.	•	ne and oestrogen are animal	hormones cutokines helps	in root development			
34.	The centre of sense of sm		monnos, egrenmico neipe	mroot development.			
	(1) Midbrain	(2) Olfactory lobes	(3) Cerebellum	(4) Cerebrum			
Ans.	(2)	•					
Sol.	Olfactory lobes regulates t	he emotional behaviour an	d sense of smell in brain.				
35 .	The component of blood	responsible for transpoting	O_2 is				
	(1) RBC	(2) WBC	(C) Platelets	(4) All of these			
Ans.	(1)						
Sol.	The component of blood	responsible for transpoting	${\rm O_2}$ is RBC, as it contains	haemoglobin which have 97%			
	affinity towards \mathcal{O}_2 .						
<i>36.</i>	Concnetration of urine depends on the presence of						
Ans.	(1) Thyroxin (3)	(2) Vasopressin	(3) ADH	(4) Melatonin			

37 .	maintains concentration of urine. Antioxidatn vitamin is						
37.	(1) 'A'	(2) 'E'	(3) 'C'	(4) All of these			
Ans.							
Sol.	Reason : Vitamin 'C' (Ascorbic acid) is a redox catalyst which can reduce and there by neutralize reactive oxygen						
	species such as hydrogen	$\operatorname{peroxide}\left(\boldsymbol{H}_{2}\boldsymbol{O}_{2}\right)$					
38.	Sardar Sarovar Dam bui	lt on river					
	(1) Sutlej	(2) Ganga	(3) Kaveri	(4) Narmada			
Ans.	(4)						
Sol.		dam built on river Narmada					
39.	Where is the cradle of hu		(0) 4	(4) • 6			
A	(1) Asia	(2) America	(3) Australia	(4) Africa			
Ans. Sol.	, ,	ed in Africa was the oldest o	no.				
<i>40.</i>		ed in Airica was the oldest o considered seat of intelligen					
10.	(1) Cerebrum	(2) Cerebellum	(3) Medulla	(4) All of thease			
Ans.		()					
41.	If α , β be the zeros of the polynomial $2x^2 + 5x + k$ such that $\alpha^2 + \beta^2 + \alpha\beta = \frac{21}{4}$, then $K = ?$						
	(1) 3	(2) -3	(3) –2	(4) 2			
Sol.	$2x^2 + 5x + K$						
	α , β are the zeros. So, $\alpha + \beta = -\frac{5}{2}$, $\alpha\beta = \frac{K}{2}$						
	$\therefore \alpha^2 + \beta^2 + \alpha\beta = \frac{21}{4} \implies \alpha^2 + \beta^2 + 2\alpha\beta - \alpha\beta = \frac{21}{4}$						
	$\Rightarrow (\alpha + \beta)^2 - \alpha\beta = \frac{21}{4} \Rightarrow \left(-\frac{5}{2}\right)^2 - \frac{K}{2} = \frac{21}{4}$						
	$\Rightarrow \frac{25}{4} - \frac{21}{4} = \frac{K}{2} \Rightarrow$	$\frac{4}{4} = \frac{K}{2} \implies K = 2$		option (4) is correct			
42 .	The sum of three consecutive terms of an AP is 21 and the sum of the squares of these terms is 165 . The middle term of the three terms is :						
	(1) 10	(2) 4	(3) 6	(4) 7			
Sol.	Let, three terms of an AI	P be $a-d$, a , $a+d$					
	\therefore sum, $(a-d)+(a)$	$+(a+d)=21$ \Rightarrow $3a$	$=21 \implies a=7$				
	Middle term $a = 7$ option (4) is correct						
43 .	If the sum of the first " p " terms of an AP is the same as the sum of its first " q " terms (where $p \neq q$) then sum						
	of $(p+q)$ th terms is :						

Sol. Reason: Antidiuretic hormone (ADH) increases absorption of water in DCT and collecting duct and there by

(3)
$$p + q - 1$$

(4)
$$p+q+1$$

Sol.
$$S_p = \frac{p}{2} [a + (p-1)d]$$

$$S_q = \frac{q}{2} [a + (q-1)d]; \quad p \neq a$$

$$\therefore S_p = S_q \qquad \Rightarrow \frac{p}{2} \left[a + (p-1)d \right] = \frac{q}{2} \left[a + (a-1)d \right]$$

$$\Rightarrow ap + p^2d - pd = aq + q^2d - qd$$

$$\Rightarrow a(p-q) + d(p^2 - q^2) - d(p-q) = 0 \qquad(1)$$

$$S_{p+q} = \frac{(p+q)}{2} \left[a + (p+q-1)d \right] \qquad \dots (2)$$

By equation (1)

$$\Rightarrow a(p-q)+d(p-q)(p+q)-d(p-q)=0$$

$$\therefore p \neq q \qquad \Rightarrow a + d(p+q) - d = 0 \qquad \Rightarrow a + (p+q-1)d = 0$$

.: By equation (2)

$$\Rightarrow S_{p+q} = 0$$

option (2) is correct

44. If
$$x^2 - 3x + 1 = 0$$
, then the value of $x^5 + \frac{1}{x^5}$?

(4)201

Sol.
$$x^2 - 3x + 1 = 0$$
 divided by x

$$x-3+\frac{1}{x}=0$$
 $\Rightarrow x+\frac{1}{x}=3$

....(1)

By squaring
$$x^2 + \frac{1}{x^2} + 2 = 9$$

$$\Rightarrow x^2 + \frac{1}{x^2} = 7$$

....(2)

By cubing of equation (1),
$$x^3 + \frac{1}{x^3} + 3\left(x + \frac{1}{x}\right) = 27$$

$$\Rightarrow x^3 + \frac{1}{r^3} = 27 - 3(3)$$
 $\Rightarrow x^3 + \frac{1}{r^3} = 18$ (3)

By equation (2) & (3),
$$\left(x^5 + \frac{1}{x^5}\right) + \left(x + \frac{1}{x}\right) = 7 \times 18$$

$$\therefore x^5 + \frac{1}{x^5} = 126 - 3 = 123$$

option (2) is correct

45. If $\frac{xy}{x+v} = a$, $\frac{yz}{x+z} = b$ and $\frac{yz}{v+z} = c$. Where a, b, c are non-zero numbers, then the value of x?

(1)
$$\frac{2abc}{ab+ac-bc}$$
 (2) $\frac{2ab}{ac+bc-ab}$ (3) $\frac{abc}{ab+bc+ac}$ (4) $\frac{2abc}{ab+bc-ac}$

(2)
$$\frac{2ab}{ac+bc-ab}$$

(3)
$$\frac{abc}{ab+bc+ac}$$

$$(4) \frac{2abc}{ab+bc-ac}$$

Sol. $\frac{x+y}{xv} = \frac{1}{a}$

$$\Rightarrow \frac{1}{y} + \frac{1}{x} = \frac{1}{a}$$

....(1)

$$\frac{x+z}{xz} = \frac{1}{b}$$

$$\Rightarrow \frac{1}{z} + \frac{1}{x} = \frac{1}{b}$$

....(2)

$$\frac{y+z}{yz} = \frac{1}{c}$$

$$\Rightarrow \frac{1}{z} + \frac{1}{y} = \frac{1}{c}$$

....(4)

Equation (1), (2) & (3), $2\left(\frac{1}{r} + \frac{1}{v} + \frac{1}{z}\right) = \left(\frac{1}{a} + \frac{1}{b} + \frac{1}{c}\right)$

$$\Rightarrow \frac{2}{x} + 2 \left\lceil \frac{y+z}{vx} \right\rceil = \frac{1}{a} + \frac{1}{b} + \frac{1}{c} \quad \Rightarrow \frac{2}{x} = \left(\frac{1}{a} + \frac{1}{b} + \frac{1}{c} \right) - 2 \left(\frac{1}{c} \right) = \frac{1}{a} + \frac{1}{b} - \frac{1}{c}$$

$$\Rightarrow \frac{2}{x} = \frac{bc + ac - ab}{abc} \quad \therefore x = \frac{2abc}{bc + ac - ab}$$

$$\therefore x = \frac{2abc}{bc + ac - ab}$$

option (2) is correct

If $\tan \theta + \cot \theta = 2$, then the value of $\tan^{23} \theta + \cot^{23} \theta = \dots$

(4)2

 $\tan \theta + \cot \theta = 2$

$$\tan \theta + \frac{1}{\tan \theta} = 2$$
, let $\tan \theta = x$ $\Rightarrow x + \frac{1}{x} = 2$ $\Rightarrow x^2 - 2x + 1 = 0$

$$\Rightarrow (x-1)^2 = 0 \Rightarrow x = 1 \therefore \tan \theta = 1 \Rightarrow \cot \theta = 1$$

$$\therefore \tan^{23}\theta + \cot^{23}\theta = 1^{23} + 1^{23} = 2$$

option (4) is correct

47. The value of $\frac{1}{1+\cot^2\alpha} + \frac{1}{1+\tan^2\alpha}$ is:

(2)
$$\frac{1}{2}$$

(3)
$$\frac{1}{4}$$

Sol.
$$\frac{1}{1+\cot^2\alpha} + \frac{1}{1+\tan^2\alpha} \implies \frac{1}{1+\frac{1}{\tan^2\alpha}} + \frac{1}{1+\tan^2\alpha}$$

$$\Rightarrow \frac{\tan^2 \alpha}{1 + \tan^2 \alpha} + \frac{1}{1 + \tan^2 \alpha} \Rightarrow \frac{\tan^2 \alpha + 1}{1 + \tan^2 \alpha} = 1$$

option (1) is correct

48. If
$$\cos 43^\circ = \frac{x}{\sqrt{x^2 + y^2}}$$
, then the value of $\tan 47^\circ$:

$$(1) \frac{x}{y} \qquad (2) \frac{y}{x}$$

$$(2) \frac{y}{x}$$

$$(3) \frac{x}{\sqrt{x^2 + y^2}}$$

(3)
$$\frac{x}{\sqrt{x^2 + y^2}}$$
 (4) $\frac{y}{\sqrt{x^2 + y^2}}$

Sol.
$$\cos 43^\circ = \frac{x}{\sqrt{x^2 + y^2}}$$
 $\Rightarrow \sin 43^\circ = \sqrt{\frac{x^2 + y^2 - x^2}{x^2 + y^2}} = \frac{y}{\sqrt{x^2 + y^2}}$

$$\therefore \tan 47^{\circ} = \tan (90 - 43) = \cot 43^{\circ}$$

$$\therefore \cot 43^{\circ} = \frac{\cos 43^{\circ}}{\sin 43^{\circ}} = \frac{x}{\sqrt{x^2 + y^2}} \times \frac{\sqrt{x^2 + y^2}}{y} = \frac{x}{y}$$

option (1) is correct

49. If
$$\sin 7x = \cos 11x$$
, then the value of $\tan 9x + \cot 9x$:

(4)3

Sol.
$$\sin 7x = \cos 11x$$
,

$$\cos(90-7x) = \cos 11x$$

$$(\because \cos(90-\theta) = \sin\theta)$$

or
$$90-7x=11x$$
 $\Rightarrow 90=18x$ $\Rightarrow x=5^{\circ}$

$$\Rightarrow 70 = 10x \Rightarrow x = 3$$

Now,
$$\tan 9x + \cot 9x = \tan 45^{\circ} + \cot 45^{\circ} = 1 + 1 = 2$$

option (2) is correct

50. If
$$\cos(\alpha + \beta) = 0$$
, then $\sin(\alpha - \beta) = ?$

(1)
$$\cos 2\beta$$

(2)
$$\cos \beta$$

(3)
$$\sin \alpha$$

(4)
$$\sin 2\alpha$$

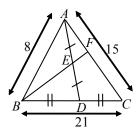
Sol.
$$\cos(\alpha + \beta) = 0$$
 $\Rightarrow \cos(\alpha + \beta) = \cos\frac{\pi}{2}$

$$\therefore \alpha + \beta = \frac{\pi}{2} \text{ or } \alpha + \beta = 90^{\circ} \implies \alpha = 90 - \beta$$

Now,
$$\sin(\alpha - \beta) = \sin(90 - \beta - \beta) = \sin(90 - 2\beta) = \cos 2\beta$$

option (1) is correct

51. In $\triangle ABC$, AD is median and E is the mid-point of AD. If BE is extended, it meets AC in F. AB=8 cm, BC=21 cm and AC=15 cm, then AF=?



- (1) 7 cm
- (2) 3 cm
- (3) 12 cm
- (4) 5 cm

Sol. Darw $DG \parallel BF$. Now, $\triangle ADG$, E is mid-point

and $\mathit{EF} \parallel \mathit{DG}$, so by converse of mid-point theorem.

F is mid-point of AG . So, AF = FG

....(1)

Also, in $\triangle BFC$, D is mid-point, $DG \parallel BF$

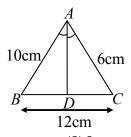
So, by converse of mid-point theorem, G is mid-point of FC

$$\therefore FG = GC \qquad ...(2)$$

By, (1) & (2),
$$AF = FG = GC$$
 $\therefore AF = \frac{1}{3}AC = \frac{1}{3} \times 15 = 5$ cm

option (4) is correct

52. In the given figure, AD is the bisector of $\angle BAC$. If AB = 10 cm, AC = 6 cm and BC = 12 cm, find BD:



- (1) 4.5 cm
- (2) 9 cm
- (3) 7.5 cm
- (4) 3 cm

Sol. $\frac{BD}{DC} = \frac{10}{6}$. Let $\frac{BD}{DC} = \frac{x}{y}$

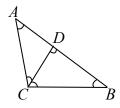
$$\Rightarrow \frac{x}{y} = \frac{5}{3} \quad \Rightarrow y = \frac{3x}{5}, \quad BD + DC = 12$$

So,
$$x + \frac{3x}{5} = 12$$
 $\Rightarrow x \left[\frac{5+3}{5} \right] = 12$ $\Rightarrow x = \frac{12 \times 5}{8}$

$$\Rightarrow x = \frac{15}{2}$$
 $\Rightarrow x = 7.5 \text{ cm}.$

option (3) is correct

In the given figure, $\angle ACB = 90^{\circ}$ and $CD \perp AB$, then:



- (1) $CD^2 = BD \cdot AD$ (2) $BC^2 = AD \cdot BD$ (3) $AC^2 = AD \cdot BC$ (4) $AD^2 = CD \cdot BD$

Sol. In $\triangle BCD \sim \triangle ACD$ (by A A similarity)

$$\therefore \frac{CD}{BD} = \frac{AC}{BC} = \frac{AD}{CD} \qquad \therefore \quad CD^2 = BD \times AD$$

$$\therefore CD^2 = BD \times AD$$

option (1) is correct

54. $\triangle ABC$ is a right triangle in which $\angle C = 90^{\circ}$ and $CD \perp AB$. If BC = a, AC = b, AB = c and CD = p,

$$(1) \ p^2 = a^2 + b^2$$

(1)
$$p^2 = a^2 + b^2$$
 (2) $\frac{1}{p^2} = \frac{1}{a^2} + \frac{1}{b^2}$ (3) $\frac{1}{c^2} = \frac{1}{a^2} + \frac{1}{b^2}$ (4) none of these

(3)
$$\frac{1}{c^2} = \frac{1}{a^2} + \frac{1}{b^2}$$

Sol. $\frac{1}{n^2} = \frac{1}{a^2} + \frac{1}{h^2}$

Area (ΔABC) = area (ΔABC)

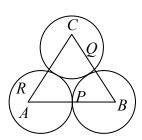
$$\Rightarrow \frac{1}{2} \times a \times b = \frac{1}{2} \times p \times C \quad \Rightarrow \frac{1}{p} = \frac{C^2}{a^2 b^2} \quad \Rightarrow \frac{1}{p^2} = \frac{a^2 + b^2}{a^2 b^2} \quad (\because a^2 + b^2 = c^2)$$

$$(:: a^2 + b^2 = c^2)$$

$$\Rightarrow \frac{1}{p^2} = \frac{a^2}{a^2b^2} + \frac{b^2}{a^2b^2} \qquad \Rightarrow \frac{1}{p^2} = \frac{1}{a^2} + \frac{1}{b^2}$$

option (2) is correct

In the given figure, three circles with centres A, B, C respectively touch each other externally. If $AB = 5 \, \mathrm{cm}$, BC = 7 cm and CA = 6 cm, then the radius of the circle with centre A is:



- (1) 1.5 cm
- (2) 2 cm
- (3) 2.5 cm
- (4) 3 cm

Sol.
$$AB = R_1 + R_3 = 5$$
(1)

$$BC = R_2 + R_3 = 7$$
(2)

$$AC = R_1 + R_2 = 6$$
(3)

By, adding equation (1), (2) & (3), $(R_1 + R_2 + R_3) = 18$

$$\Rightarrow R_1 + R_2 + R_3 = 9 \qquad \Rightarrow R_1 + 7 = 9$$

$$\therefore R_1 = 2 \text{ cm}$$
 option (2) is correct

56. In the given figure ABCD is a square of side 14 cm. Find the area of the shaded region.



- $(1) 56 \text{ cm}^2$
- $(2) 48 \text{ cm}^2$
- $(3) 42 \text{ cm}^2$
- $(4) 44 \text{ cm}^2$
- **Sol.** Required shaded region, area of (ABCD) area of 4 small circles

$$= 14 \times 14 - 4 \times \pi r^{2} = 14 \times 14 - 4 \times \frac{22}{7} \times \frac{7}{2} \times \frac{7}{2}$$

$$=196-154=42 \text{ cm}^2$$

option (3) is correct

- **57.** A metallic spherical shell of internal and external diameters 4 cm and 8 cm respectively, is melted and recast into the form of a cone of base diameter 8 cm. The height of the cone is:
 - (1) 12 cm
- (2) 14 cm
- (3) 15 cm
- (4) 18 cm

Sol. Volume (spherical shell) = volume (cone)

$$\Rightarrow \frac{4}{3}\pi \left(R^3 - r^3\right) = \frac{1}{3}\pi r_1^2 h \qquad \Rightarrow 4\left(4^3 - 2^3\right) = 4 \times 4 \times h$$

$$\Rightarrow 4(64-8) = 4 \times 4 \times h \Rightarrow 56 = 4h$$

$$\Rightarrow h = \frac{56}{4} = 14$$
cm

option (2) is correct

- **58.** In what ratio is the line segment joining the points A(-2, -3) and B(3, 7) divided by the y-axis.
 - (1) 3 : 2

(2) 2 : 3

- (3) 1:5
- (4) 2:5

Sol. Let y -axis divide AB in the ratio k:1.

So, by section formula, co-ordinate of p is $\left(\frac{3k-2}{k+1}, \frac{7k-3}{k+1}\right)$

As, y -axis have, 0 is x -coordinate.

	$\therefore \frac{3k-2}{k+1} = 0 \Rightarrow \frac{2}{3}$:1 ⇒2:3		optio	n (2) is correct	
<i>5</i> 9.	Two coins are tossed sin	nultaneously. What is the pr	obability of getting at least	one head.		
	(1) $\frac{1}{4}$	(2) $\frac{1}{2}$	(3) $\frac{3}{4}$	(4) 1		
Sol.	$S = \{HH, HT, TH,$	TT }				
	Event for atleast one he	$ad = \{HH, HT, TH\}$				
	$\therefore P$ (getting atleast or	the head) = $\frac{3}{4}$		option	n (3) is correct	
<i>60.</i>	The relation between m	ean, mode and median is :				
	$(1) Mode = 3 \times Mean - 2$	2×Median	(2) Mode = $3 \times$ Median -	-2×Mean		
	(3) Mean = $3 \times$ Median -	-2×Mode	(3) Median = $3 \times$ Mean -	-2×Mode		
Sol.	$Mode = 3 \times Median - 2 \times 3 \times$	(Mean		option	n (2) is correct	
61.	Who was the Governor	General of India in 1857?				
	(1) Wellesley	(2) Dalhousie	(3) Canning	(4) Minto		
Ans.	(3)					
Sol.	. Selected by lord Palmerston to succeed lord Dalhousie .					
62 .	Who was the First India	n Woman President in the Ir	ndian National Congress?			
	(1) Mrs. Annie Besanat		(2) Sucheta Kripalani			
	(3) Sarojini Naidu		(4) Indira Gandhi			
Ans.	(3)					
Sol.	In 1925 she presided over	Kanpur session				
63 .	Who penned the followi	_				
		ab hamare dil me hai, Dekl				
	(1) Bismil	(2) Raj Guru	(3) Bhagat Singh	(4) Azad		
Ans.	• /					
Sol.	-	ong in Urdu at Patna 1921				
64 .	(1) 1855	annexed into British domir	ion in the year (2) 1854	(3) 18	356(4) 1853	
Ans.	, ,		(2) 1004	(0) 10	1000	
Sol.		ruler and it was annexed un	der the pretext of doctrine of	of lapse.		
65 .						
	(1) U.S.A.	, Savar part	(2) Germany	(3) Spain	(4) France	
Ans.	, ,			, , 1	, ,	
	• /	Hardayal, it had its branc	h at Canada also			

(2) Gorakhpur

(3) Maharajganj

(4)

66.

(1) Deoria

Chauri Chaura is situated in the District of

	Kushinagar						
Ans.	(2)						
Sol.	A place in united province	ce where non-cooperation r	movement turned violent				
67 .	The British Parliament p	assed the Regulating Act to	o improve the ad ministratio	n of the East India Company in			
	the year						
	(1) 1773	(2) 1775	(3) 1853	(4) 1855			
Ans.	(1)						
Sol.	The Regulating Act o	f 1773 was an Act of the	Parliament of Great Britai	in intended to overhaul the			
	management of the Ea	st India Company's rule in	<u>India .</u>				
<i>68</i> .	The First English factory	in India was established a	t				
	(1) Bombay	(2) Hooghly	(3) Surat	(4) Calcutta			
Ans.	(2)						
Sol.	The first English factory	was set up on the banks of	river hooghly in 1651.				
<i>69</i> .	The Asiatic Society of B	engal was founded by					
	(1) Raja Ram Mohan Ro	у	(2) Sir William Jones				
	(3) W. W. Hunter		(4) William Bentinck				
Ans.	s. (2)						
Sol.	The Asiatic Society v	vas founded by Sir William	<u> Jones</u> on 15 Janu ary 1784	1			
70 .	The founder of the autor	nomous kingdom of Avadh	ı was				
	(1) Ahmad Shah Abdali		(2) Safdarjung				
	(3) Saadat Khan Burhar	n UI-Mulk	(4) Zulfiqur Khan				
Ans.	Ans. (3)						
71 .	The permanent Settleme	ent of 1793 vested the own	ership of land in :				
	(1) Individual peasants		(2) Zamindars				
	(3) Village communities		(4) State				
Ans.	(2)						
Sol.	The Permanent Set	tlement — also known	as the Permanent Set	tle ment of <u>Bengal</u> — was			
	an <u>agreement</u> between the <u>East India Company</u> and <u>Bengali</u> landlords to fix revenues to be raised from land.						
72 .	The year of Great Divide	e in Indian Demographic hi	story is				
	(1) 1921	(2) 1947	(3) 1951	(4) 1982			
Ans.	(1)						
Sol.	. The year 1921 is taken as the demographic divide for the reason that before this year, the population was not						
	stable, sometimes it in c	reased and at other times it	decreased.				
73 .	Who is the first woman	Prime Minister of India?					
	(1) Meira Kumar	(2) Sonia Gandhi	(3) Indira Gandhi	(4) Annie Besant			
Ans.	(3)						
74 .	Lenin was born in the ye	ear					

5. The My Lai massacre occurred in

(2)1880

Sol. Alias Lenin was a Russian communist revolutionary, politician, and political theorist

(1) 1870

Ans. (1)

(3) 1885

(4) 1890

(1) 1964 (2) 1966 (3) 1968 (4) 1970

Ans. (3)

Sol. The **My Lai Massacre**, the <u>Vietnam War</u> mass killing of 347 and 504 unarmed civilians in <u>South Vietnam</u> on March 16, 1968.

76. Assertion(A): Cotton textile industry is decentralised in India

Reaason (R): Cotton textile industry is immesssely by market.

Select the correct option from the given alternatives

(1) Both (A) and (R) are true, and (R) explains (A)

(2) Both (A) and (R) are trure but (R) does not explain (A)

(3) (A) is true and (R) is false

(4) (A) is false and (R) is true

Ans. (1)

77. Assertion (A): Public transport is given preference over private vehicles in large urban cities

Reason (R): Large number of private vehicles in urban area cause trffic congestion and pollution.

Select the correct option from the given alternatives

(1) Both (A) and (R) are true, and (R) explains (A)

(2) Both (A) and (R) are trure but (R) does not explain (A)

(3) (A) is true and (R) is false

(4) (A) is false and (R) is true

Ans. (2)

78. Assertion (A): india is rich in biodiversity

Reason (R): It is situtated in tropical area

Select the corrrect option from the given alternatives

(1) Both (A) and (R) are true, and (R) explains (A)

(2) Both (A) and (R) are trure but (R) does not explain (A)

(3) (A) is true and (R) is false

(4) (A) is false and (R) is true

Ans. (1)

79. Assertion (A): Oil refineries in India area mostly along the sea coast

Reason (R): The climate along the sea coast is very congenial

Select the correct option from the given alternatives

(1) Both (A) and (R) are true, and (R) explains (A)

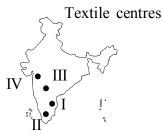
(2) Both (A) and (R) are trure but (R) does not explain (A)

(3) (A) is true and (R) is false

(4) (A) is false and (R) is true

Ans. (2)

80. Match the textile centres indicated on the map of India (I,II,III & IV) with their representative names



	(A) Chennai	(B) Solapur	(C) Coimbatore	(D) Mumbai		
	(1) I C II B III A IV D	(2) II C I A IV D III B	(3) III D IIC I A IV B	(4) IV C IIIA IIB ID		
Ans.	(2)					
81 .	In south India, which soil is extensively found					
	(1) Laterite	(2) Red soil	(3) Black cotton soil	(4) Alluvial soil		
Ans.	(2)					
82 .	Which of the following is a	an example of non-metallic	mineral			
	(1) Gold	(2) Bauxite	(3) Graphite	(4) Tin		
Ans.	0					
83 .	Which chemical is affecting	ng fertility in frog communit	ty			
	(1) Bengin	(2) Urea	(3) Andrin	(4) Phosphorus		
Ans.	(NA)					
84 .	Which is the first expressy	vay of India				
	(1) Delhi - Kolkata	(2) Mumbai-Pune	(3) Pune-Chennai	(4) Delhi-Mumabi		
Ans.	(2)					
Sol.	The Mumbai Pune Exp	ressway , (officially known a	as			
	the YashwantraoChava	ın Mumbai Pune Express	sway) is India's first six-lane	concrete, high-speed, access		
	controlled tolled expressw	<u>ray</u>)				
85 .	Over exploitation of unde	rground water has led to in	crease in con centration of l	Fluoride in which state?		
	(1) Bihar	(2) Jharkhand	(3) Assam	(4) Sikkim		
Ans.						
86 .	Capital of Lakshdweep is					
	(1) Kavaratti	(2) Daman	(3) Silvassa	(4) Port Blair		
Ans.						
87 .	Production of wheat is high					
	(1) Punjab	(2) Haryana	(3) Uttar Pradesh	(4) Madhya Pradesh		
Ans.						
88.	Which mine is found in KI		10.			
	(1) Copper Mines	(2) Lignite Mines	(3) Bauxite Mines	(4) Iron Ore Mines		
Ans.						
89.	What is the longitudinal e		(0) (500515 11 0 00	AALE .		
	(1) 60° 10' East to 96° 2		(2) 67°05' East to 96°2			
•	(3) 69°05' East to 98°	22' East	(4) 68°08' East to 97°.	25'East		
Ans. 90.		he youngest structure of In	dia? (2) Shiwalik Range (4) penisular India			
Ans.		11				
91.	Panchayati Raj System is (1) Centralisation of powe (2) Decentralisation of powe (3) Co-operation with peo (4) All of the above	er wer				
Ans	• •					

 $\textbf{Sol.} \quad \text{The } \textbf{\textit{Panchayati Raj}} \ \ \text{in India generally refers to the} \ \ \underline{\text{system}} \ \ \text{introduced by constitutional amendment in 1992} \ .$

92 .	A member of Rajya Sabha is elected						
	(1) For six year ((2) For five year	(3) For four year	(4) No definite period			
Ans.	ns. (1)						
93 .	Who appoints the Chief Ele	ctron Commissioner of In	dia?				
	1) Prime Minister (2) President						
	(3) parliament		(4) Chairman of Lok Sabl	ha			
Ans.	(2)						
94.	In India the maximum num	ber of Lok sabha and Raj	iya Sabha members may be	е			
	(1) 500 and 250		(2) 525 and 238				
	(3) 537 and 275		(4) 552 and 250				
Ans.	(4)						
Sol.	The maximum strength of the	e House envisaged by the	Constitution of India is 552,	The Rajya Sabha or Council			
	of States is the upper hou	use of the Parliament of	<u>India</u> . Membership of Rajya	a Sabha is lim ited by the Con-			
	stitution to a maximum of 2	250 members .					
95 .	The time period of Dr. A.P.	J Abdul Kalam as a Presid	dent of India is				
	(1) 25 July 2000 to 25 July	2005	(2) 25 July 2001 to 25 Jul	ly 2006			
	(3) 25 July 2002 to 25 July	2007	(4) 25 July 2003 to 25 Jul	ly 2008			
Ans.	(3)						
Sol.	$11^{ ext{th}}$ president of india .						
96 .	The most appropriate meas	ture of a country's econon	nic growth is				
	(1) Gross Domestic Product		(2) Net Domestic Product				
	(3) Net National Product		(4) Per Capita Product				
Ans.	(1)						
Sol.	GDP (gross domestic produ	ucts)					
97.	Finance is distributed between	een the centre and states o	on the recom mendations o	f which of the following?			
	(1) Planning commission		(2) Public Accounts Comr	mittee			
	(3) Finance Commission		(4) National Development Council				
Ans.	(3)						
Sol.	Distribution of net proceeds o	of taxes between Centre a	nd the States, to be divided	as per their respective contribu-			
	tions to the taxes.						
98.	The first Agricultural Univer	sity of the country is					
	(1) J.N.K.V., Jabalpur		(2) G.B.P.A.U, Panth Nag	gar			
	(3) P.A.U., Ludhiana		(4) R.A.U., Bikaner				
Ans.							
Sol.	Govindballabh pant agricultural university.						
99 .	Who amongst the following is the current president of the World Bank						
		(2) Lewis Preston	(3) Barber Conable	(4) None of these			
Ans.	, ,						
Sol.							
100.	When was the National Dev	relopment Council formed					
	(1) 26th January, 1950		(2) 15th March, 1950				
•	(3) 6th August, 1951		(4) 6th August, 1952				
Ans.	(4)						